$$\sum_e a_{ie}^{\phi} m_i^{\phi} \chi_e = \sum_i \Gamma_i^{\phi}$$