$$\frac{\partial}{\partial t}\left(\frac{d^2\phi}{dy^2} - k^2\phi\right) + ikU\left(\frac{d^2\phi}{dy^2} - k^2\phi\right) + ik\frac{dQ}{dy}\phi = 0$$