$$(U-c)\left(\frac{d^2\phi}{dy^2}-k^2\phi\right)+\left(\beta-\frac{d^2U}{dy^2}\right)\phi=0$$

where $c\equiv\dfrac{\omega}{k}$